

## Data-Aware Tuning of Deep Learning Models

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## Outline

#### Introduction

- Current Trends
- Research Goals

#### Autowave

- Radar Waveform Design Overview
- "Lean Neural Networks for Autonomous Radar Waveform Design"
- "Lean Neural Networks for Real-time Embedded Spectral Notching Waveform Design"

#### SNN-GAN

- Spiking Neural Networks (SNNs) Overview
- Generative Adversarial Networks (GANs) Overview
- "Toward Robust Spiking Neural Networks"
- "Dataset Augmentation for Robust Spiking Neural Networks"

#### Current & Future Work



- Neural Network (NN) popularity growing very quickly [1]
- NN boasts superb non-linear function approximation [2, 3, 4] applied to many domains





#### Introduction Current Trends

- NN dataset size growing [5]
- NN model size growing [6]







- Harder problem  $\rightarrow$  more data  $\rightarrow$  larger model
- "1000 typewriting monkeys vs 1 Shakespeare"

Output

Softmax

Linear

LaverNorm

Dropout

Input

Embedding

Input

- Trend is to keep adding blocks to black-box model
- Are they all necessary? •
- Could design fewer more . intelligent modules









- Leverage extant problem information
- Reduce model footprint
- Reduce data footprint



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#### Current & Future Work



#### Increased Wireless Spectrum Interference

- 4G/5G telecommunication networks
- Mobile sensors
- IoT devices







Interference Mitigation with Spectral Notching

- Sample RF environment
- Determine interfered stopband
- Modify transmit waveform to avoid stopband





- Difficult task with multiple constraints that must be met for radar functionality and power efficiency
- Trade-off between runtime/power and precision
  - Want near real-time without sacrificing performance





- Solutions must also be portable to different hardware
  - RFSoC FPGA (Radio Frequency System on Chip Field-Programmable Gate Array) has fixed-point representation limit for example



Work	Low SWaP	End-to-End	Hardware Portability	"Intelligent Design"
Error Reduction Algorithm (ERA) [7]		Х		Х
Re-Iterative Uniform Weight Optimization Algorithm (RUWO) [8]		Х		Х
MIMO GPU [9]		Х	Х	Х
TCNRWR [9]	Х		Х	Х
RVTDCNN [10]	Х	Only output	Х	
Autowave pre- computed [11, 12, 13]	Х		Х	
Autowave [AB1, AB2]	X	X	X	X



- AutoWave → Artificial Intelligence (AI) implementation of an adaptive radar system which uses NN to adjust transmitted waveforms to avoid sources of interference
  - Treat RUWO as absolute, train NN to learn RUWO
- Naïve approach of simply throwing a larger NN will not work

Algorithm	GPU Lat	ency (µs)	CPU Lat	$ency (\mu s)$	Cosin	e Similarity	Null Dep	oth (dBm)
NN MSE 1 Layer NN MSE 2 Layers NN MSE 3 Layers	$747.71 \pm 749.40 \pm 797.72 \pm$	$5.23 \\ 5.61 \\ 10.03$	$786.44 \pm 797.92 \pm 855.34 \pm$	5.01 5.99 6.38	0.9901 0.9900 0.9898	$\pm 7.69 \times 10^{-5}$ $\pm 7.89 \times 10^{-5}$ $\pm 9.87 \times 10^{-5}$	$28.54 \pm 29.17 \pm 26.57 \pm$	0.16 0.22 0.23



Moving away from Mean Squared Error (MSE)

Numerical comparisons between coefficient vectors prone to errors





#### Tailor loss function to radar waveform design

- 1. Provide quicker learning to <u>valid</u> solutions compared to MSE
- 2. Encourage NN to always produce <u>valid</u> waveforms (even if not identical to RUWO)
- 3. Discourage "close enough" waveforms which are similar but not valid



**AutoWave** 

#### Split processing into 2 parallel NN

Quadrature radar waveforms are <u>separate</u>



I Amplitude (V)	Q Amplitude (V)	I+Q			
		Amplitude (V)	Phase (°)		
1	0	1	0		
0	1	1	90		
-1	0	1	180		
0	-1	1	270		



#### Split processing into 2 parallel NN (cont'd)



#### **CPU / GPU Simulation**

Algorithm	Cosine Similarity	Null Depth (dBm)
RUWO	$1.0 \pm 0.0$	$202.23 \pm 0.0$
ERA	$0.9982 \pm 0.0$	$31.89 \pm 0.0$
NN MSE	$0.9901~\pm~7.69\times10^{-5}$	$28.54 \pm 0.16$
NN Custom Loss	$0.9789\pm9.53\times10^{-5}$	$22.32 \pm 0.13$
NN Split	$0.9900~\pm~1.08\times10^{-4}$	$29.75 \pm 0.12$

#### **RFSoC FPGA Open-Air Trials**

Algorithm	Null Depth (dBm)
RUWO	$33.62 \pm 0.041$
ERA	$37.13 \pm 0.057$
NN MSE	$28.17 \pm 0.213$
NN Custom Loss	$21.22 \pm 0.138$
NN Split	$28.93 \pm 0.285$

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#### **AutoWave**

#### "Lean Neural Networks for Autonomous Radar Waveform Design"





**Custom Loss** 



**MSE** 







Algorithm	CPU Later	ncy ( $\mu s$ )	GPU La	ter	ncy ( $\mu$ s)	RFSoC Lat	enc	y (µs)
RUWO	$806,347.0 \pm$	11,860.82	649,581.0	±	33,168.78	10,060,000.0	±	999.0
$\mathbf{ERA}$	$166,982.0 \pm$	3465.06	641,441.0	±	20,921.13	1246.0	±	8.8
NN MSE	$786.4 \pm$	5.01	747.71	±	5.23	21.7	±	0.0
NN Custom Loss	$762.8 \pm$	5.04	735.68	±	7.99	21.7	±	0.0
NN Split	$1931.5~\pm$	9.75	823.63	±	6.76	13.7	±	0.0





Specifically target low power embedded devices (Raspberry Pi 3B)





Algorithm	Dell r <sup>2x Intel E5-2670, NVIDIA C Latency (ms)</sup>	720 GT 1030, 144GB RAM Energy (J)	Raspberry Pi 3BBroadcom BCM2837, 1GB RAMLatency (ms)Energy (J		
RUWO	$1064.98 \pm 10.94$	$261.3\pm6.5$	$453,\!965.43\pm4131.61$	$1510.5\pm14.8$	
ERA	$185.47\pm3.87$	$45.5\pm1.4$	$1982.04 \pm 29.27$	$6.5\pm0.1$	
NN MSE	$23.19 \pm 1.86$	$\textbf{3.7} \pm \textbf{0.3}$	$\textbf{230.98} \pm \textbf{2.74}$	$\textbf{0.6} \pm \textbf{0.01}$	
NN Tailored Loss Function	$\textbf{20.72} \pm \textbf{0.44}$	3.7 ± 0.1	$233.92\pm3.16$	$\textbf{0.6} \pm \textbf{0.01}$	
NN Tailored Network Architecture	$23.35\pm0.29$	$4.1\pm0.6$	$250.90\pm0.63$	$0.7\pm0.01$	



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## Spiking Neural Networks (SNNs)

- Biologically inspired 3<sup>rd</sup> generation neural networks
- Neurons communicate via discrete pulses over time
- Great for time-series data
- SNN processing consumes less power when realized on neuromorphic hardware such as Intel Loihi [15]



https://www.intel.com/content/www/us/en/newsroom/news/intel-unveils-neuromorphic-loihi-2-lava-software.html#gs.4ve63w



## ANNs vs

- Operate on continuous values  $x_1, x_2, ..., x_n$
- Information propagates
   instantaneously



## SNNs

- Operate on discrete spike trains  $S_1, S_2, \dots, S_n$
- Must be run over a period of time





Spiking Neural Networks (SNNs) Overview

#### ANNs vs

$$E = L(y, \hat{y})$$
  

$$net_j = \sum_i w_{ij} x_i + b$$
  

$$o_j = \varphi(net_j)$$

$$\delta_{j} = \begin{cases} \frac{\partial L(y,o_{j})}{\partial o_{j}} \frac{d\varphi(net_{j})}{dnet_{j}} & j \text{ output} \\ \left(\sum_{k} w_{jk} \delta_{k}\right) \frac{d\varphi(net_{j})}{dnet_{j}} & j \text{ hidden} \end{cases}$$
$$\Delta w_{ij} = -\eta o_{j} \delta_{j}$$

SNNs Input  $s_i(t) = \sum_f \delta(t - t_i^{(f)})$  $a_{i}(t) = (\epsilon * s_{i})(t) \quad \epsilon^{(t)} = \frac{t}{\tau_{c}} exp\left(1 - \frac{t}{\tau_{c}}\right) \Theta(t)$  $v_i(t) = (v * s)(t)$   $v_{(t)} = -2\vartheta exp(1-\frac{t}{\tau_n})\Theta(t)$  $u(t) = \sum_{i} w_{i} a_{i}(t) + v_{i}(t)$  $f_s(u): u \to s$  $s(t) \coloneqq s(t) + \delta(t - t^{(f+1)})$  $t^{(f+1)} = \min\{t : u(t) = \vartheta, t > t^{(f)}\}$ u(t)θ  $u_{rest}$ 26 refractory period

## SNN Data

- SNNs operate on discrete spike trains
- Can be either generated from static data using integrate-and-fire (IF) neurons or captured directly using a Dynamic Vision Sensor (DVS) camera which produces event data:

[*x* coordinate, *y* coordinate, *t* timestep, *p* polarity of light – intensity change]



## **Spike Distribution Dependencies**

- For a given static image, there are a copious number of valid spike trains which can be created/captured depending on IF neuron parameters, DVS camera settings, or lighting properties of the subject
- Surrogate gradient SNN training can fixate on the intervals of training spikes leading to generalization

issues



## Our approach

- Using a spiking <u>GAN</u>, generate valid samples of varying spike distributions
- Augmented dataset provides additional robustness against samples different from the original training set
- Generated samples enrichen dataset without additional manual collection of data (and exponential growth for each different spike distribution)

Generative Adversarial Networks (GANs)

- Adversarial learning paradigm in which a generator model G synthesizes artificial samples, and a discriminator model *D* classifies samples as either real or fake
- G and D "compete" against each other i.e., they are High playing a minimax Dimensional Sample game to each better Real Space Real Samples Discriminator themselves Model



### Why GANs

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- Most models are classifiers e.g., given an input x, they predict a label y thus estimating P(y|x)
- However, these models cannot estimate P(x) and therefore cannot sample from P(x) i.e., they cannot create new samples
- The combination of a traditional classifier model with a new generative model unlocks new functionality

#### Generator

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• The generator *G*, often a deep neural network, transforms an input noise vector into a realistic sample

The goal of *G* is to learn a mapping from some noisy space  $p_z$  to  $p_g$  which approximates the real data distribution  $p_{data}$ 

• Once sufficiently trained,  $p_g \approx p_{data}$  e.g., *G* can generate arbitrary samples which appear to be real

### Discriminator

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- The discriminator *D*, often a deep neural network or Convolutional Neural Network (CNN) for images, classifies input samples as either real (coming from the real distribution) or fake (coming from *G*)
- The goal of *D* is to learn a mapping from an input space (containing potentially both real & fake samples) to [0, 1] where 0 asserts a sample is fake and 1 asserts a sample is real

### GAN Training

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- *G* and *D* are trained simultaneously in which *D* identifies areas in which it can more easily identify fake samples
- These areas then become the focus for where *G* updates its weights
- Given sufficient capacity, *G* and *D* converge to where  $p_g \approx p_{data}$  and D(x) = 0.5 for all input



### GAN Training (cont'd)

• For fixed *G*, training *D* to the optimal classifier  $D_G^*(x) = \frac{p_{data}(x)}{p_{data}(x) + p_a(x)}$  is

computationally expensive. Instead, training of G and D is alternated

while keeping *D* near optimal to give *G* better gradients [16]

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• **Notice:** *G* is never trained directly on the real data, it only learns from the gradient from *D* flowing backward. This prevents "overfitting" and instead allows *G* to branch beyond the real data

Algorithm 1 Minibatch stochastic gradient descent training of generative adversarial nets. The number of steps to apply to the discriminator, k, is a hyperparameter. We used k = 1, the least expensive option, in our experiments.

for number of training iterations do

- for k steps do
  - Sample minibatch of m noise samples  $\{z^{(1)}, \ldots, z^{(m)}\}$  from noise prior  $p_g(z)$ .
  - Sample minibatch of m examples  $\{x^{(1)}, \ldots, x^{(m)}\}$  from data generating distribution  $p_{\text{data}}(x)$ .
  - Update the discriminator by ascending its stochastic gradient:

$$\nabla_{\theta_d} \frac{1}{m} \sum_{i=1}^m \left[ \log D\left( \boldsymbol{x}^{(i)} \right) + \log \left( 1 - D\left( G\left( \boldsymbol{z}^{(i)} \right) \right) \right) \right].$$

#### end for

- Sample minibatch of m noise samples  $\{z^{(1)}, \ldots, z^{(m)}\}$  from noise prior  $p_g(z)$ .
- Update the generator by descending its stochastic gradient:

$$\nabla_{\theta_g} \frac{1}{m} \sum_{i=1}^m \log\left(1 - D\left(G\left(\boldsymbol{z}^{(i)}\right)\right)\right).$$

#### end for

The gradient-based updates can use any standard gradient-based learning rule. We used momentum in our experiments.

### GAN Training Issues

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- "Helvetica Scenario" aka Mode Collapse
  - Situation in which *G* fails to generalize its outputs and instead produces all similar samples
  - Often caused by *G* learning too fast relative to *D*, and so *G* begins to favor generating a subset of the data but is unable to escape the local minima once *D* continues learning
- Vanishing Gradient
  - Often caused by *D* learning too fast relative to *G* in which *D* can perfectly distinguish real/fake samples leaving *G* unable to "catch up" in its generating ability leading to stagnation in *G*

#### Balancing *G* and *D* is difficult!

#### Extensions

- Conditional GAN (CGAN)
  - Allows for specifying which class of data to be generated by attaching a label to the latent input vector for *G*





## Our approach (rep.)

- Using a spiking <u>GAN</u>, generate valid samples of varying spike distributions
- Augmented dataset provides additional robustness against samples different from the original training set
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- (1) SNN classifier trained to convergence
- (2) GAN trained using classifier weights to seed discriminator
- (3) Trained GAN generator used to augment train dataset for further classifier training





## Our approach (cont'd)

- During augmentation, samples are generated on an as-needed basis determined by the relative class performances
- Difficulty of correct classification is not uniform across all classes of data → disproportionate number of samples can achieve same overall accuracy



## Our approach (cont'd)

- Three schemes used to determine the number of additional samples needed for the next iteration:
  - 1) equal: same number of samples across all classes
  - 2) **adhoc**: only samples from the 3 worst performing classes added
  - 3) **scale**: number of samples added correlated to relative performance of each class

## Setup

- SLAYER [17] SNN training platform used
- CIFAR-10 training spike trains generated from X~U(100, 200) firing rate distribution using LIF (leaky integrate-and-fire neuron) in Nengo [18] simulator
- Models evaluated on **fewer** spikes and **more** spikes distributions  $\rightarrow$  half ( $X \sim U(50, 100)$ ) and double ( $X \sim U(200, 400)$ ) the number of spikes compared to training distribution



## Training

• Our models quickly responded to the changing spike distribution



## Testing

- All models perform worse as samples drifted further from the training distribution
- Our models outperformed baseline classifier by an average 1.80% and had an average 1.02% lesser reduction in accuracy

Model	<b>Testing Spike Distribution</b>						
MOGEI	Fewer Spikes	Train Dist. Spikes	More Spikes				
Baseline	$37.76 \pm 0.34$	$52.67 \pm 0.31$	$42.73 \pm 0.52$				
Our approach [equal]	$39.09 \pm 0.25$	54.57 ± 0.27	$44.07 \pm 0.52$				
Our approach [adhoc]	39.33 ± 0.28	$54.25 \pm 0.30$	$44.67 \pm 0.52$				
Our approach [scale]	$38.52 \pm 0.39$	$54.05 \pm 0.32$	$43.51 \pm 0.29$				

## Outcomes

- Conventional SNN training methods do not ensure generalization capabilities for temporal data
- Our results show improvements in model robustness against dissimilar samples from the training data



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#### Current & Future Work

"Generative Datasets for Training Spiking Neural Networks"

- Expand datasets (N-MNSIT, CIFAR10-DVS, DVSGesture)
- Expand frameworks (Nengo Neural Engineering Framework )





**Current Work** 

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**Current Work** 

#### **Spatial Splitting**



#### **Temporal Splitting**



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- Why do NN models (including SNNs) need so much data?
- NN training has many pitfalls [19, 20], better algorithm must exist (Foutse Khomh)
- MAJOR dependency on training data
  - Model performs poorly
     ↓
     Test set representative?

$$E = L(y, \hat{y})$$
  

$$net_j = \sum_i w_{ij} x_i + b$$
  

$$o_j = \varphi(net_j)$$

$$\delta_{j} = \begin{cases} \frac{\partial L(y,o_{j})}{\partial o_{j}} \frac{d\varphi(net_{j})}{dnet_{j}} & j \text{ output} \\ \left(\sum_{k} w_{jk} \delta_{k}\right) \frac{d\varphi(net_{j})}{dnet_{j}} & j \text{ hidden} \end{cases}$$
$$\Delta w_{ij} = -\eta o_{j} \delta_{j}$$



#### Dataset condensation [21]

 Rather than generating realistic samples, generate "super" samples which don't necessarily look real, but produce identical gradient updates <u>faster</u>





#### **Future Work**







Kangaroo

Orange

Orchid

Pine Tree

Tulip



Apple



Goose

Camel

Guacamole

German Shepard

Red Panda

Potpie

Ladybug

Triumphal Arch



Guinea Pig





Clock









Siamese Cat

Pear







Banana

Church

Sheepdog

Flamingo

French Horn

Golden Retriever

King Penguin

Strawberry

Tiger

# What about for SNNs?



- Can our GAN approach be combined with dataset condensation to generate "super" samples?
- Can this approach be applied to neuromorphic computing to compress the already larger data-space?
- Can this approach condense different spike distributions?



## Questions?



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